Chapter 17

Process Fault Tolerance

17.1 Introduction

Long running and large scale applications are at increased risk of encountering process failures during normal execution. We consider a process failure as a fail-stop failure; failed processes become permanently unresponsive to communications. This chapter introduces the MPI features that support the development of applications and libraries that can tolerate process failures. The approach described in this chapter is intended to prevent the deadlock of processes while avoiding impact on the failure-free execution of an application.

The expected behavior of MPI in the case of a process failure is defined by the following statements: any MPI operation that involves a failed process must not block indefinitely, but either succeed or raise an MPI exception (see Section 17.2); an MPI operation that does not involve the failed process will complete normally, unless interrupted by the user through provided functionality. Asynchronous failure propagation is not required. If an application needs global knowledge of failures, it can use the interfaces defined in Section 17.3 to explicitly propagate locally detected failures.

This chapter does not define process failure semantics for the operations specified in Chapters [10,][11][and 13], therefore they remain undefined by the MPI standard.

An implementation that does not tolerate process failures must provide the interfaces and semantics defined in this chapter, but must never raise an exception of class MPI_ERR_PROC_FAILED or MPI_ERR_PENDING related to process failure (as defined below).

Advice to users. Many of the operations and semantics described in this chapter are only applicable when the MPI application has replaced the default error handler MPI_ERRORS_ARE_FATAL on, at least, MPI_COMM_WORLD. (*End of advice to users.*)

17.2 Failure Notification

This section specifies the behavior of an MPI communication operation when failures occur on processes involved in the communication. A process is considered involved in a communication if any of the following is true:

1. the operation is collective and the process appears in one of the groups of the associated communication object; 24

³⁰ ticket327. ³¹ ticket325.

 32 ticket 326.

 33 ticket0.

	538		CHAPTER 17.	PROCESS FAULT TOLERANCE
1 2	-	process is a specified or cation;	matched destination	or source in a point-to-point com-
3 4 5		peration is an MPI_ANY e source group.	_SOURCE receive oper	ation and the failed process belongs
6 7 8		, .		d process (such as a point-to-point return a process failure error.
9 10 11 12 13 14	tion other opera migh	only for processes invol failures until necessary ations, it may choose to	ved in an ongoing op 7. Moreover, as long a delay returning an e	entation may provide failure detec- beration, and postpone detection of as an implementation can complete rror. Another valid implementation ickly as possible. (<i>End of advice to</i>
15 16 17 18				about process failures during initia- corresponding completion function
19 20	17.2.1 St	artup and Finalize		
21 22 23 24 25	comp MPI_	olete the MPI_INIT succ	essfully, then a high e reporting of the pr	MPI_INIT but its peers are able to quality implementation will return cocess failure to a subsequent MPI
ticket0. 26	MPI_F failures.	INALIZE will complete	[succesfully]successfu	ally even in the presence of process
27 28 29 30 31 32 33 34 34 35	Advi MPI_ MPI voke AppI MPI_	COMM_WORLD may have only provides failure d d and provides no supplications are encouraged	e failed before, during etection capabilities port for fault toleran to implement all ra	etion 8.7, the process with rank 0 in g, or after the call to MPI_FINALIZE. up to when MPI_FINALIZE is in- ince during or after MPI_FINALIZE. ank-specific code before the call to 0 in MPI_COMM_WORLD fails. (<i>End</i>
³⁶ ticket0. ³⁷	17.2.2 P	oint-to-Point and Colled	ctive Communication	
38 39 40 41 42 43 44 ticket0. 45 46 47 48	to-point co MPI_ERR_F this comm The co following to was able to has been r failure at request is a	PROC_FAILED. Future p unicator must also return ompletion of a nonblock hree error codes due to o complete despite the far natched with the send, the sender. MPI_ERR_F	nunication is marked oint-to-point commu m MPI_ERR_PROC_FA ing receive from MPI_ process failure. MPI ailure. MPI_ERR_PRO but cannot complete PENDING indicates th continued. To ackno	ANY_SOURCE can return one of the _SUCCESS is returned if the receive C_FAILED indicates that the request [succesfully]successfully due to the nat while a process has failed, the owledge a failure and discover which
	Processes 1	and, the user bround of		

17.2. FAILURE NOTIFICATION

1 Advice to implementors. $\mathbf{2}$ MPI libraries can not determine if the completion of an unmatched reception operation 3 of type MPI_ANY_SOURCE can succeed when one of the potential senders has failed. If 4 the operation has matched, it is handled as a named receive. If the operation has not 5yet matched and was initiated by a nonblocking communication call, then the request 6 is still valid and pending and it is marked with an error of class MPI_ERR_PENDING. 7 In all other cases, the operation must return MPI_ERR_PROC_FAILED. 8 (End of advice to implementors.) 9 ¹⁰ ticket0. 11 When the failure of a process involved in a communication operation is discovered by the 12MPI implementation before the successful completion of the operation, the communication 13 completion function must raise one of the following error classes: 14• MPI_ERR_PENDING indicates that the communication is a non-blocking operation and 15neither the operation nor the request identifying the operation are completed. Two 16 circumstances can raise this exception: another communication raised an exception 17 (as defined in Section 3.7.5); or the communication is a receive operation from 18 MPI_ANY_SOURCE and no matching send has been posted. 19 20• In all other cases, the operation must raise an exception of class 21MPI_ERR_PROC_FAILED which indicates that the failure prevents the operation from 22following its failure-free specification. If there is a request identifying the communi-23cation operation, it is completed. 24Advice to users. 2526To acknowledge a failure and discover which processes failed, the user should call 27MPI_COMM_FAILURE_ACK (as defined in Section 17.3.1). 28(End of advice to users.) 29 When a communication operation raises an exception related to process failure, any 30 output buffers are *undefined*. 31 When a collective operation cannot be completed because of the failure of an involved 32 process, the collective operation [eventually] returns an error of class ³³ ticket0. MPI_ERR_PROC_FAILED. [The content of the output buffers is *undefined*.] ³⁴ ticket0. 35 Advice to users. 36 Depending on how the collective operation is implemented and when a process fail-37 ure occurs, some participating alive processes may raise an exception while other 38 processes return successfully from the same collective operation. For example, in 39 MPI_BCAST, the root process may succeed before a failed process disrupts the oper-40 ation, resulting in some other processes returning an error. However, it is noteworthy 41 that for [non-rooted] collective operations on an intracommunicator in which all pro-42 ticket0. $_{43}$ ticket0. cesses contribute to the result and all processes receive the result, processes which do not enter the operation due to process failure provoke all surviving ranks to return 44 MPI_ERR_PROC_FAILED. Similarly, for a non-rooted the same collective operations on 45 ticket0. an intercommunicator, a process in the remote group which failed before entering the 46operation has the same effect on all surviving ranks of the local group. 47

(End of advice to users.)

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1	Advice to users.		
2	Note that communicator creation functions (like MPI_COMM_DUP or		
3 4	MPI_COMM_SPLIT) are collective operations. As such, if a failure happened during		
5	the call, an error might be returned to some processes while others succeed and ob-		
6	tain a new communicator. While it is valid to communicate between processes which		
7	succeeded to create the new communicator, it is the responsibility of the user to en- sure that all involved processes have a consistent view of the communicator creation,		
8	if needed. A conservative solution is to have each process either revoke (see Sec-		
9	tion 17.3.1) the parent communicator if the operation fails, or call an MPI_BARRIER on		
10 11	the parent communicator and then revoke the new communicator if the MPI_BARRIER		
12	fails.		
13	(End of advice to users.)		
ticket 327. $_{14}$			
15 16	17.2.3 Dynamic Process Management		
17	Dynamic process management functions require some additional semantics from the MPI		
18	implementation as detailed below.		
19 20	1. If the MPI implementation returns an error related to process failure to the root process		
20	of MPI_COMM_CONNECT or MPI_COMM_ACCEPT, at least the root processes of		
22	both intracommunicators must return the same error of class MPI_ERR_PROC_FAILED		
23	(unless required to return $MPI_ERR_REVOKED$ as defined by $17.3.1$).		
24	2. If the MPI implementation returns an error related to process failure to the root process		
25 26	of MPI_COMM_SPAWN, no spawned processes should be able to communicate on the		
27	created intercommunicator.		
28	Advice to users. As with communicator creation functions, it is possible that if a		
29	failure happens during dynamic process management operations, an error might be		
30 31	returned to some processes while others succeed and obtain a new communicator.		
ticket $325.$ ³¹	(End of advice to users.)		
33			
34	17.2.4 One-Sided Communication		
35	As with all nonblocking operations, one-sided communication operations should delay all		
36 37	failure notification until their synchronization operations which may return		
38	MPI_ERR_PROC_FAILED (see Section 17.2). If the implementation returns an error related		
39	to process failure from the synchronization function, the epoch behavior is unchanged from the definitions in Section 11.4. As with collective operations over MPI communicators, it is		
40	possible that some processes have detected a failure and returned MPI_ERR_PROC_FAILED,		
41	while others returned MPI_SUCCESS.		
42 43	Unless specified below, the state of memory targeted by any process in an epoch in		
44	which operations completed with an error related to process failure is undefined.		
45	1. If a failure is to be reported during active target communication functions		
46	MPI_WIN_COMPLETE or MPI_WIN_WAIT (or the non-blocking equivalent		
47 48	MPI_WIN_TEST), the epoch is considered completed and all operations not involving		
40	the failed processes must complete successfully.		

2. If the target rank has failed, MPI_WIN_LOCK and MPI_WIN_UNLOCK operations return an error of class MPI_ERR_PROC_FAILED. If the owner of a lock has failed, the lock cannot be acquired again, and all subsequent operations on the lock must fail with an error of class MPI_ERR_PROC_FAILED.

Advice to users. It is possible that request-based RMA operations complete successfully while the enclosing epoch completes in error due to process failure. In this scenario, the local buffer is valid but the remote targeted memory is undefined. (*End of advice to users.*)

17.2.5 I/O

I/O error classes and their consequences are defined in [s]Section 13.7. The following section defines the behavior of I/O operations when MPI process failures prevent their successful completion.

Since collective I/O operations may not synchronize with other processes, process failures may not be reported during a collective I/O operation. If a process failure prevents a file operation from completing, an MPI exception of class MPI_ERR_PROC_FAILED is raised.

Once an MPI implementation has returned an error of class MPI_ERR_PROC_FAILED, the state of the file pointer is *undefined*.

Advice to users.

Users are encouraged to use MPI_COMM_AGREE on a communicator containing the same group as the file handle, to deduce the completion status of collective operations on file handles and maintain a consistent view of file pointers.

(End of advice to users.)

17.3 Failure Mitigation Functions

17.3.1 Communicator Functions

MPI provides no guarantee of global knowledge of a process failure. Only processes involved in a communication operation with the failed process are guaranteed to eventually detect its failure (see Section 17.2). If global knowledge is required, MPI provides a function to revoke a communicator at all members.

MPI_COMM_REVOKE(comm)				
IN	comm	communicator (handle)		
MPI_COMM_H	omm_revoke(MPI_Comm comm) REVOKE(COMM, IERROR) ER COMM, IERROR			

This function notifies all processes in the groups (local and remote) associated with the communicator comm that this communicator is now considered revoked. This function 48

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¹⁰ ticket326.

 $_{14}$ ticket0.

1is not collective and therefore does not have a matching call on remote processes. It is ticket0. $\mathbf{2}$ erroneous to call MPI_COMM_REVOKE on a communicator for which no operation raised 3 an MPI exception related to process failure. All alive processes belonging to comm will be 4 notified of the revocation despite failures. Revocation of a communicator completes any $\mathbf{5}$ non-local MPI operations on comm with error and causes any new operations to complete 6 with error, with the exception of MPI_COMM_SHRINK and MPI_COMM_AGREE (and its $\overline{7}$ nonblocking equivalent). A communicator becomes revoked as soon as: 8 1. MPI_COMM_REVOKE is locally called on it; 9 10 2. Any MPI operation completed with an error of class MPI_ERR_REVOKED because an-11 other process in comm has called MPI_COMM_REVOKE. 12Once a communicator has been revoked, all subsequent non-local operations on that 13 communicator, with the exception of MPI_COMM_SHRINK and MPI_COMM_AGREE (and 14its nonblocking equivalent), are considered local and must complete with an error of class 15MPI_ERR_REVOKED. 1617 Advice to users. High quality implementations are encouraged to do their best to 18 free resources locally when the user calls free operations on revoked communication 19objects, or communication objects containing failed processes. (End of advice to 20users.) 2122 23MPI_COMM_SHRINK(comm, newcomm) 24 25IN communicator (handle) comm 26OUT newcomm communicator (handle) 2728int MPI_Comm_shrink(MPI_Comm comm, MPI_Comm* newcomm) 2930 MPI_COMM_SHRINK(COMM, NEWCOMM, IERROR) 31 INTEGER COMM, NEWCOMM, IERROR 32 This collective operation creates a new intra or inter communicator newcomm from the 33 revoked intra or inter communicator comm respectively by excluding its failed processes as 34 detailed below. It is erroneous MPI code to call MPI_COMM_SHRINK on a communicator 35 which has not been revoked (as defined above) and will return an error of class 36 MPI_ERR_ARG. 37 This function must not return an error due to process failures (error classes 38 MPI_ERR_PROC_FAILED and MPI_ERR_REVOKED). All processes that succeeded agreed on 39 the content of the group of processes that failed. This group includes at least every process 40 failure that has raised an MPI exception of class MPI_ERR_PROC_FAILED or 41 MPI_ERR_PENDING. The call is semantically equivalent to an MPI_COMM_SPLIT operation 42that would succeed despite failures, and where living processes participate with the same 43 color, and a key equal to their rank in comm and failed processes implicitly contribute 44MPI_UNDEFINED. 4546 Advice to users. This call does not guarantee that all processes in newcomm are 47 alive. Any new failure will be detected in subsequent MPI operations. (End of advice 48 to users.)

MPI_COMM_FAILURE_ACK(comm)					
IN	comm	communicator (handle)	2 3		
			4		
int MPI_(Comm_failure_ack(MP	I_Comm comm)	5		
МРТ СОММ	_FAILURE_ACK(COMM,	TEBBUB)	6		
	GER COMM, IERROR		7		
			8		
	* 0	the users a way to <i>acknowledge</i> all locally notified failures on	9		
comm. After the call, unmatched MPI_ANY_SOURCE receptions that would have returned					
an error code due to process failure (see Section 17.2.2) proceed without further reporting of errors due to those acknowledged failures.					
01 011015 0	fue to those acknowled	ged failules.	12		
Adva	ice to users. Calling N	IPI_COMM_FAILURE_ACK on a communicator with failed	13 14		
proc	esses does not allow a	that communicator to be used successfully for collective	15		
*		nmunication on a communicator with acknowledged fail-	16		
		rn an error of class MPI_ERR_PROC_FAILED as defined in	17		
	°	v use collective operations on a communicator with failed	18		
-	,	br should first be revoked using MPI_COMM_REVOKE and should be created using MPI_COMM_SHRINK. (<i>End of</i>	19		
	ce to users.)	should be created using MFI_COMM_SHRINK. (End of	20		
aacı	ee to users.)		21		
			22		
			23 24		
MPI_CON	IM_FAILURE_GET_AC	KED(comm, failedgrp)	25		
IN	comm	communicator (handle)	26		
OUT	failedgrp	group of failed processes (handle)	27		
			28		
int MPI_(Comm_failure_get_ac	ked(MPI_Comm comm, MPI_Group* failedgrp)	29		
МРТ СОММ	FAILURE GET ACKED(COMM, FAILEDGRP, IERROR)	30		
	GER COMM, FAILEDGRP		31		
	-		32 33		
	*	s the group failedgrp of processes, from the communicator	34		
,		acknowledged as failed by preceding calls to he new group failed grp can be empty, that is, equal to	³⁵ ticket0.		
	JP_EMPTY.	the new grouppanedgrp can be empty, that is, equal to	36		
			37		
		、 、	38		
MPI_COMM_AGREE(comm, flag)			39		
IN	comm	communicator (handle)	40		
INOUT	flag	boolean flag	41		
			42 43		
int MPI_(Comm_agree(MPI_Comm	comm, int * flag)	43		
ů ů					
MPI_COMM_AGREE(COMM, FLAG, IERROR) LOGICAL FLAG					
INTEGER COMM, IERROR					

1 2 ticket0. 3 4 5 6 7 8 9 10 11 12 13	On complete a logical '2 error due to and process If com the valuess operation) Advi	This function performs a collective operation on the group of living processes in comm. On completion, all living processes must agree to set the output value of flag to the result of a logical 'AND' operation over the in[t]put values of flag. This function must not return an error due to process failure (error classes MPI_ERR_PROC_FAILED and MPI_ERR_REVOKED), and processes that failed before entering the call do not contribute to the operation. If comm is an intercommunicator, the value of flag is a logical 'AND' operation over the values contributed by the remote group (where failed processes do not contribute to the operation). Advice to users. MPI_COMM_AGREE maintains its collective behavior even if the comm is revoked. (End of advice to users.)			
14	MPI_COM	MPI_COMM_IAGREE(comm, flag, req)			
15 16	IN	comm		communicator (handle)	
17	INOUT	flag		boolean flag	
18	OUT	req		request (handle)	
19 20		·		- 、 /	
21	int MPI_C	<pre>int MPI_Comm_iagree(MPI_Comm comm, int* flag, MPI_Request* req)</pre>			
22	MPI_COMM_	IAGREE(COMM, F	LAG, REQ, II	ERROR)	
23 24		CAL FLAG			
25	INTEGER CUMM, REQ, IERRUR				
26		function has the s	same semanti	cs as MPI_COMM_AGREE except that it is non-	
ticket325. 27	0				
28 29	17.3.2 One-Sided Functions				
30					
31					
32 33	MPI_WIN_	_REVOKE(win)			
34	IN	win		window (handle)	
35					
36	int MPI_V	<pre>Nin_revoke(MPI_</pre>	Win win)		
37 38		REVOKE(WIN, IER			
39	This function notifies all processes within the window win that this window is now considered revoked. A revoked window completes any non-local MPI operations on win				
40					
41 42					
42	revoked, all subsequent non-local operations on that window are considered local and must				
44	fail with an error of class MPI_ERR_REVOKED.				
45					
46	46 47 48				

MPI_WIN_GET_FAILED(win, failedgrp)			
IN	win	window (handle)	2
			3
OUT	failedgrp	group of failed processes (handle)	4
			5
int MPL_	Win_get_failed()	MPI_Win win, MPI_Group* failedgrp)	6
MPI_WIN_	GET_FAILED(WIN,	FAILEDGRP, IERROR)	7
INTE	GER COMM, FAILE	DGRP, IERROR	8
Thia	local an anation not	und the mean feiled run of an economy from the mindom win which	9 10
This local operation returns the group failedgrp of processes from the window win which are locally known to have failed.			
are locally	y KHOWH to Have la	uleu.	11 12
Adv	vice to users. M	PI makes no assumption about asynchronous progress of the	13
failı	re detection. A va	alid MPI implementation may choose to only update the group	14
of lo	ocally known failed	l processes when it enters a synchronization function. (End of	15
adv	ice to users.)		16
A da	nice to meens. It is	possible that only the calling process has detected the reported	17
		vledge is necessary, processes detecting failures should use the	18
	<u> </u>	KED. (End of advice to users.)	19
Call			20 ticket 326.
			21
17.3.3 I	/O Functions		22
			23
			24
MPI_FILE	E_REVOKE(fh)		25
IN	fh	file (handle)	26
			27
int MDT	File_revoke(MPI	File fb)	28 29
IIIC MFI_	LITE TEADYE (HLT		30
	_REVOKE(FH, IER	ROR)	31
INTE	GER FH, IERROR		32
This	function notifies a	all ranks within file fh that this file handle is now considered	33
revoked.			34
	oing non-local com	pletion operations on a revoked file handle raise an exception	35
		Once a file handle has been revoked, all subsequent non-local	36
		e must raise an MPI exception of class MPI_ERR_REVOKED.	37
			38
17.4 E	Fror Codes and	Classes	39
11.7 L			40
The follow	wing error classes a	are added to those defined in Section 8.4:	41
0			
17 E Examples			
17.5 Examples			
17.5.1 Master/Worker			
The example below presents a master code that handles failures by ignoring failed pro-			
cesses and resubmitting requests. It demonstrates the different failure cases that may occur			

```
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                                         CHAPTER 17. PROCESS FAULT TOLERANCE
1
               MPI_ERR_PROC_FAILED
                                       The operation could not complete because
2
                                       of a process failure (a fail-stop failure).
3
               MPI_ERR_REVOKED
                                       The communication object used in the op-
                                       eration has been revoked.
4
5
6
                   Table 17.1: Additional process fault tolerance error classes
7
8
     when posting receptions from MPI_ANY_SOURCE as discussed in the advice to users in Sec-
9
     tion 17.2.2.
10
11
                      Fault-Tolerant Master Example
     Example 17.1
12
13
     int master(void)
14
     ſ
15
         MPI_Comm_set_errhandler(comm, MPI_ERRORS_RETURN);
16
         MPI_Comm_size(comm, &size);
17
18
         /* ... submit the initial work requests ... */
19
         MPI_Irecv( buffer, 1, MPI_INT, MPI_ANY_SOURCE, tag, comm, &req );
20
21
22
         /* Progress engine: Get answers, send new requests,
23
             and handle process failures */
24
         while( (active_workers > 0) && work_available ) {
25
              rc = MPI_Wait( &req, &status );
26
27
              if( (MPI_ERR_PROC_FAILED == rc) || (MPI_ERR_PENDING == rc) ) {
28
                  MPI_Comm_failure_ack(comm);
29
                  MPI_Comm_failure_get_acked(comm, &g);
30
                  MPI_Group_size(g, &gsize);
31
32
                  /* ... find the lost work and requeue it ... */
33
34
                  active_workers = size - gsize - 1;
35
                  MPI_Group_free(&g);
36
37
                  /* repost the request if it matched the failed process */
38
                  if( rc == MPI_ERR_PROC_FAILED )
39
                      MPI_Irecv( buffer, 1, MPI_INT, MPI_ANY_SOURCE,
40
                                  tag, comm, &req );
41
                  }
42
43
                  continue;
44
              }
45
46
              /* ... process the answer and update work_available ... */
47
              MPI_Irecv( buffer, 1, MPI_INT, MPI_ANY_SOURCE, tag, comm, &req );
48
         }
```

```
/* ... cancel request and cleanup ... */
}
```

17.5.2 Iterative Refinement

The example below demonstrates a method of fault-tolerance to detect and handle failures. At each iteration, the algorithm checks the return code of the MPI_ALLREDUCE. If the return code indicates a process failure for at least one process, the algorithm revokes the communicator, agrees on the presence of failures, and later shrinks it to create a new communicator. By calling MPI_COMM_REVOKE, the algorithm ensures that all processes will be notified of process failure and enter the MPI_COMM_AGREE. If a process fails, the algorithm must complete at least one more iteration to ensure a correct answer.

Example 17.2 Fault-tolerant iterative refinement with shrink and agreement

```
16
while( gnorm > epsilon ) {
                                                                                     17
    /* Add a computation iteration to converge and
                                                                                     18
       compute local norm in lnorm */
                                                                                     19
    rc = MPI_Allreduce( &lnorm, &gnorm, 1, MPI_DOUBLE, MPI_MAX, comm);
                                                                                     20
                                                                                     21
    if( (MPI_ERR_PROC_FAILED == rc ) ||
                                                                                     22
        (MPI_ERR_COMM_REVOKE == rc) ||
                                                                                     23
        (gnorm <= epsilon) ) {</pre>
                                                                                     ^{24}
                                                                                     25
        if( MPI_ERR_PROC_FAILED == rc )
                                                                                     26
            MPI_Comm_revoke(comm);
                                                                                     27
                                                                                     28
        /* About to leave: let's be sure that everybody
                                                                                     29
            received the same information */
                                                                                     30
        allsucceeded = (rc == MPI_SUCCESS);
                                                                                     31
        MPI_Comm_agree(comm, &allsucceeded);
                                                                                     32
        if( !allsucceeded ) {
                                                                                     33
             /* We plan to join the shrink, thus the communicator
                                                                                     34
                should be marked as revoked */
                                                                                     35
            MPI_Comm_revoke(comm);
                                                                                     36
            MPI_Comm_shrink(comm, &comm2);
                                                                                     37
            MPI_Comm_free(comm); /* Release the revoked communicator */
                                                                                     38
             comm = comm2;
                                                                                     39
             gnorm = epsilon + 1.0; /* Force one more iteration */
                                                                                     40
        }
                                                                                     41
    }
                                                                                     42
}
                                                                                     43
```